

Functional Generation of Harmony and Melody

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An extremely useful model of musical harmony



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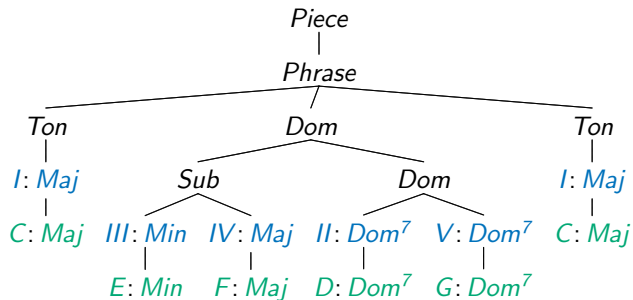
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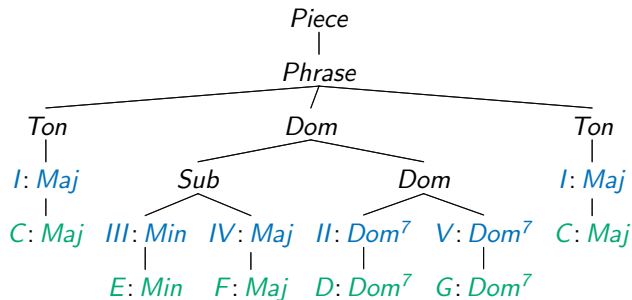
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- ▶ FCOMP: a system for automatic generation of harmony and accompanying melody (this talk).

An example: visualising harmonic structure



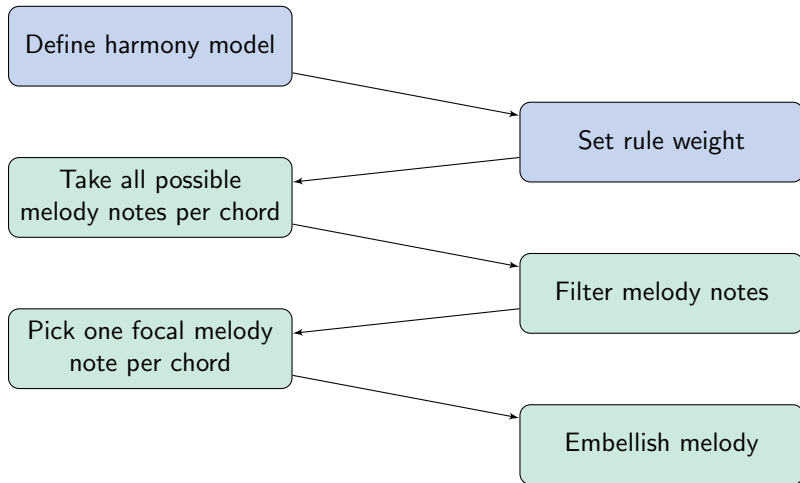
You can see this tree as having been produced by taking the chords in green as input...

An example: generating harmonic structure



You can see this tree as having been produced by taking the chords in green as input... or the chords might have been dictated by the structure!

System structure



A functional model of harmony



$Piece_{\mathfrak{M}} \rightarrow [Phrase_{\mathfrak{M}}]$ ($\mathfrak{M} \in \{Maj, Min\}$)

A functional model of harmony



$Piece_{\mathfrak{M}} \rightarrow [Phrase_{\mathfrak{M}}] \quad (\mathfrak{M} \in \{Maj, Min\})$

$Phrase_{\mathfrak{M}} \rightarrow \begin{array}{cc} Ton_{\mathfrak{M}} & Dom_{\mathfrak{M}} & Ton_{\mathfrak{M}} \\ | & & \\ & Dom_{\mathfrak{M}} & Ton_{\mathfrak{M}} \end{array}$

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$$Dom_{\mathfrak{M}} \rightarrow \begin{array}{l} V_{\mathfrak{M}}^7 \\ | \\ V_{\mathfrak{M}} \\ | \\ VII_{\mathfrak{M}}^0 \\ | \\ Sub_{\mathfrak{M}} \quad Dom_{\mathfrak{M}} \\ | \\ II_{\mathfrak{M}}^7 \quad V_{\mathfrak{M}}^7 \end{array}$$

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$$Sub_{Maj} \rightarrow \begin{array}{c} II_{Maj}^m \\ | \quad IV_{Maj} \\ | \quad III_{Maj}^m \quad IV_{Maj} \end{array}$$

$$Sub_{Min} \rightarrow IV_{Min}^m$$

$$I_{Maj} \rightarrow C: Maj$$

$$I_{Min}^m \rightarrow C: Min$$

$$V_{\mathfrak{M}}^7 \rightarrow G: Dom^7$$

$$VII_{\mathfrak{M}}^0 \rightarrow B: Dim$$

Now in Haskell—I



A GADT encoding musical harmony:

```
data Mode = MajMode | MinMode
```

```
data Piece =  $\forall \mu :: \text{Mode.Piece}$  [ Phrase  $\mu$  ]
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```

```
data Phrase ( $\mu :: \text{Mode}$ ) where
```

```
PhraseVI :: Ton  $\mu \rightarrow \text{Dom } \mu \rightarrow \text{Ton } \mu \rightarrow \text{Phrase } \mu$ 
```

```
PhraseVI :: Dom  $\mu \rightarrow \text{Ton } \mu \rightarrow \text{Phrase } \mu$ 
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data Ton ( $\mu :: \text{Mode}$ ) where
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TonMaj :: SD I Maj  $\rightarrow \text{Ton Maj}_{\text{Mode}}$ 
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A GADT encoding musical harmony:

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```

```
data Dom ( $\mu :: \text{Mode}$ ) where
```

```
Dom1 :: SD V Dom7  $\rightarrow$  Dom  $\mu$ 
```

```
Dom2 :: SD V Maj  $\rightarrow$  Dom  $\mu$ 
```

```
Dom3 :: SD VII Dim  $\rightarrow$  Dom  $\mu$ 
```

```
Dom4 :: SDom  $\mu \rightarrow$  Dom  $\mu \rightarrow$  Dom  $\mu$ 
```

```
Dom5 :: SD II Dom7  $\rightarrow$  SD V Dom7  $\rightarrow$  Dom  $\mu$ 
```

Scale degrees are the leaves of our hierarchical structure:

```
data DiatonicDegree = I | II | III | IV | V | VI | VII  
data Quality       = Maj | Min | Dom7 | Dim  
data SD ( $\delta :: \textit{DiatonicDegree}$ ) ( $\gamma :: \textit{Quality}$ ) where  
    SurfaceChord :: ChordDegree  $\rightarrow$  SD  $\delta$   $\gamma$ 
```

Generating harmony



Now that we have a datatype representing harmony sequences, how do we generate a sequence of chords?

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$$\begin{aligned} \text{gen} &:: (\text{Representable } \alpha, \text{Generate } (\text{Rep } \alpha)) \\ &\Rightarrow \text{Gen } \alpha \end{aligned}$$

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$$\begin{aligned} \text{gen} &:: (\text{Representable } \alpha, \text{Generate } (\text{Rep } \alpha)) \\ &\Rightarrow [(\text{String}, \text{Int})] \rightarrow \text{Gen } \alpha \end{aligned}$$

Examples of harmony generation—I



```
testGen :: Gen (Phrase MajMode)
testGen = gen [("Dom4", 3), ("Dom5", 4)]
example :: IO ()
example = let k = Key (Note ♮ C) MajMode
           in sample' testGen >>= mapM_ (printOnKey k)
printOnKey :: Key → Phrase MajMode → IO String
```

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printOnKey :: Key → Phrase MajMode → IO String
```

```
> example
```

```
[C: Maj, D: Dom7, G: Dom7, C: Maj]
```

```
[C: Maj, G: Dom7, C: Maj]
```

```
[C: Maj, E: Min, F: Maj, G: Maj, C: Maj]
```

```
[C: Maj, E: Min, F: Maj, D: Dom7, G: Dom7, C: Maj]
```

```
[C: Maj, D: Min, E: Min, F: Maj, D: Dom7, G: Dom7, C: Maj]
```

Examples of harmony generation—II



Generating a melody for a given harmony



We then generate a melody in 4 steps:

Generating a melody for a given harmony



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1. Generate a list of candidate melody notes per chord;

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1. Generate a list of candidate melody notes per chord;
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These four steps combine naturally using plain monadic bind:

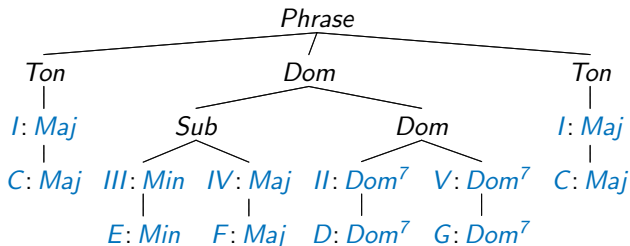
$$\begin{aligned} \text{melody} &:: \text{Key} \rightarrow \text{State MyState Song} \\ \text{melody } k &= \text{genCandidates} \gg \text{refine} \gg \text{pickOne} \gg \text{embellish} \\ &\gg \text{return} \circ \text{Song } k \end{aligned}$$

More details in the paper!

Example I



A musical score consisting of two staves. The upper staff is a treble clef with a single melodic line of eighth notes. The lower staff is a bass clef with block chords. The chords are: C major (C-E-G), F major (F-A-C), C major (C-E-G), F major (F-A-C), C major (C-E-G), and C major (C-E-G).



Conclusion



FCOMP: a *simple and easy to understand and improve* functional system for automatic generation of harmony and accompanying melody.

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Lots of room for improvement:

- ▶ Voice leading and counterpoint
- ▶ Handle repetition
- ▶ Improve embellishment
- ▶ Rhythm, form, instrumentation, dynamics

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Thank you for your attention!