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A Generic Deriving Mechanism for Haskell

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Outline

Overview

Viewpoints

End user

Compiler implementer

Library writer

Conclusion



Overview

- ▶ Haskell has a number of (built-in) type classes that can automatically be derived: `Bounded`, `Enum`, `Eq`, `Ord`, `Read`, and `Show`
- ▶ We present a mechanism that lets you define these classes and your own `in` Haskell such that they can be derived automatically
- ▶ Similar to “Derivable Type Classes”, but better integrated into Haskell
- ▶ Implemented in the Utrecht Haskell Compiler
- ▶ We describe formally how it can be implemented in other compilers



Features

We can:

- ▶ Handle meta-information such as constructor names and field labels
- ▶ Derive all the Haskell 98 classes
- ▶ Derive most of the classes that GHC can derive, including **Typeable** and classes of kind $\star \rightarrow \star$ such as **Functor**



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Using generic functions

If a class is generic, it can be used in a **deriving** construct.
Assuming a type class

```
data Bit = 0 | 1  
class Encode  $\alpha$  where  
  encode ::  $\alpha \rightarrow$  [Bit]
```

The end user can write

```
data Exp = Const Int | Plus Exp Exp  
  deriving (Show, Encode)
```

and then use

```
test :: [Bit]  
test = encode (Plus (Const 1) (Const 2))
```



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Basic idea

- ▶ For each datatype, there is an equivalent internal representation.
- ▶ All the concepts contained in the **data** construct (application, abstraction, choice, sequence, recursion) are captured by a limited set of **representation types**.
- ▶ The compiler generates an internal representation for every datatype, together with conversion functions and derived instances



Example

```
data Exp = Const Int | Plus Exp Exp
```

```
type Rep0Exp =  
  D1 $Exp ( C1 $ConstExp (Rec0 Int)  
            + C1 $PlusExp (Rec0 Exp × Rec0 Exp))
```



Example

```
data Exp = Const Int | Plus Exp Exp
```

```
type Rep0Exp =  
    ( Int  
    + ( Exp × Exp ))
```

Note that the representation is **shallow** – recursive calls are to `Exp`, not `Rep0Exp`.

Most of the representation is meta-information about:



Example

```
data Exp = Const Int | Plus Exp Exp
```

```
type RepExp0 =  
  D1 $Exp ( ( Int)  
             + ( Exp × Exp))
```

Note that the representation is **shallow** – recursive calls are to `Exp`, not `RepExp0`.

Most of the representation is meta-information about:

- ▶ the datatype itself,



Example

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data Exp = Const Int | Plus Exp Exp
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- ▶ the constructors,



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```

Note that the representation is **shallow** – recursive calls are to `Exp`, not `Rep0Exp`.

Most of the representation is meta-information about:

- ▶ the datatype itself,
- ▶ the constructors,
- ▶ where recursive calls take place.



Lifting

Our approach can handle type classes with parameters of both

- ▶ kind \star such as `Encode` and `Show`;
- ▶ kind $\star \rightarrow \star$ such as `Functor`.

We therefore represent **all** datatypes at kind $\star \rightarrow \star$.

Types of kind \star get a dummy parameter in their representation.



Representation types

data V_1 ρ

data U_1 $\rho = U_1$

data $(+)$ $\phi \psi \rho = L_1(\phi \rho) \mid R_1(\psi \rho)$

data (\times) $\phi \psi \rho = \phi \rho \times \psi \rho$

The void type V_1 is for types without constructors.

The unit type U_1 is for constructors without fields.

Sums represent choice between constructors.

Products represent sequencing of fields.



Meta-information

data $K_1 \iota \gamma \quad \rho = K_1 \gamma$

data $M_1 \iota \mu \phi \rho = M_1 (\phi \rho)$

These types record additional information, such as names and fixity, for instance. They are instantiated as follows:

data D -- datatypes

type $D_1 = M_1 D$

data C -- constructors

type $C_1 = M_1 C$

data S -- record selectors

type $S_1 = M_1 S$

data R -- recursive calls

type $Rec_0 = K_1 R$

data P -- parameters

type $Par_0 = K_1 P$

We group five combinators into two because we often do not care about all the different types of meta-information.



Example: meta-information for expressions

UHC automatically generates the following for `Exp`:

```
data $Exp
```

```
data $ConstExp
```

```
data $PlusExp
```

```
instance Datatype $Exp where
```

```
  moduleName _ = "ModuleName"
```

```
  datatypeName _ = "Exp"
```

```
instance Constructor $ConstExp where conName _ = "Const"
```

```
instance Constructor $PlusExp where conName _ = "Plus"
```

The classes `Datatype` and `Constructor` can hold more information if desired.



Conversion

We use a type class to mediate between values and representations:

class Representable₀ α τ **where**

from₀ :: $\alpha \rightarrow \tau$ χ

to₀ :: $\tau \chi \rightarrow \alpha$



Conversion

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Instance for **Exp** (automatically generated by UHC):

instance Representable₀ Exp Rep₀^{Exp} **where**

from₀ (Const n) = M₁ (L₁ (M₁ (K₁ n)))

from₀ (Plus e e') = M₁ (R₁ (M₁ (K₁ e × K₁ e')))

to₀ (M₁ (L₁ (M₁ (K₁ n)))) = Const n

to₀ (M₁ (R₁ (M₁ (K₁ e × K₁ e')))) = Plus e e'



A note on extensions

The `Representable0` class could use a functional dependency:

```
class Representable0 α τ | α → τ where ...
```

Alternatively, τ could be encoded as an associated type:

```
class Representable0 α where  
  type Rep0 α :: * → *  
  from0 :: α → Rep0 α χ  
  to0   :: Rep0 α χ → α
```

But we want to stay inside Haskell98 as much as possible. We only require support for multi-parameter type classes.



Compiler support

For each datatype, the compiler generates the following:

- ▶ Meta-information, i.e. datatypes and class instances.
- ▶ Representation type synonym(s).
- ▶ `Representable0` and/or `Representable1` instance.

For each **deriving** construct, the compiler looks for an appropriate `DERIVABLE` pragma (specified by the library writer) and generates a default instance.



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Generic function definitions

The library writer defines generic (derivable) functions.

We use two classes: one for the base types (kind \star):

```
class Encode  $\alpha$  where  
  encode ::  $\alpha \rightarrow [\text{Bit}]$ 
```

and one for the representation types (kind $\star \rightarrow \star$):

```
class Encode1  $\phi$  where  
  encode1 ::  $\phi \chi \rightarrow [\text{Bit}]$ 
```



Simple cases

The generic cases are defined as instances of Encode_1 :

instance $\text{Encode}_1 V_1$ **where**

$\text{encode}_1 _ = []$

instance $\text{Encode}_1 U_1$ **where**

$\text{encode}_1 _ = []$

instance $(\text{Encode}_1 \phi) \Rightarrow \text{Encode}_1 (M_1 \iota \gamma \phi)$ **where**

$\text{encode}_1 (M_1 a) = \text{encode}_1 a$



Sums and products

instance $(\text{Encode}_1 \phi, \text{Encode}_1 \psi) \Rightarrow \text{Encode}_1 (\phi + \psi)$ **where**
 $\text{encode}_1 (L_1 a) = 0 : \text{encode}_1 a$
 $\text{encode}_1 (R_1 a) = 1 : \text{encode}_1 a$

instance $(\text{Encode}_1 \phi, \text{Encode}_1 \psi) \Rightarrow \text{Encode}_1 (\phi \times \psi)$ **where**
 $\text{encode}_1 (a \times b) = \text{encode}_1 a \# \text{encode}_1 b$



Constants and base types

For constants, we rely on `Encode`:

```
instance (Encode  $\alpha$ )  $\Rightarrow$  Encode1 (K1  $\iota$   $\alpha$ ) where  
  encode1 (K1 a) = encode a
```

In this way we close the recursive loop: if α is a representable type, `encode` will call `from` and then `encode1` again.

For base types, we need to provide ad-hoc instances:

```
instance Encode Int where encode = ...  
instance Encode Char where encode = ...
```



Default generic instance

Every generic function needs a default case:

```
encode_Default :: (Representable0 α τ, Encode1 τ)
                ⇒ τ χ → α → [Bit]
encode_Default rep x = encode1 ((from0 x) 'asTypeOf' rep)

{-# DERIVABLE Encode encode encode_Default #-}
```



Default generic instance

Every generic function needs a default case:

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encode_Default :: (Representable0 α τ, Encode1 τ)
                ⇒ τ χ → α → [Bit]
encode_Default rep x = encode1 ((from0 x) 'asTypeOf' rep)

{-# DERIVABLE Encode encode encode_Default #-}
```

We are done:

```
data Exp = Const Int | Plus Exp Exp deriving Encode
```

will cause the generation of

```
instance Encode Exp where
```

```
    encode = encode_Default (⊥ :: RepExp0 χ)
```



Back to the internals: kind $\star \rightarrow \star$ types

For type constructors (kind $\star \rightarrow \star$), we use a few more representation types:

newtype Par_1 $\rho = \text{Par}_1 \ \rho$

newtype Rec_1 ϕ $\rho = \text{Rec}_1 \ (\phi \ \rho)$

newtype (\circ) $\phi \ \psi \ \rho = \text{Comp}_1 \ (\phi \ (\psi \ \rho))$

We use Par_1 to store the parameter, Rec_1 to encode recursive occurrences of type constructors, and \circ for type composition (eg. lists of trees).



Example: representing lists I

data List $\rho = \text{Nil} \mid \text{Cons } \rho \text{ (List } \rho)$
deriving (Show, Encode, Functor)

The compiler generates instance of `Representable0` for kind \star functions:

type Rep₀^{List} $\rho =$
D₁ \$List (C₁ \$Nil_{List} U₁
+ C₁ \$Cons_{List} (Par₀ $\rho \times \text{Rec}_0 \text{ (List } \rho)$))

instance Representable₀ (List ρ) (Rep₀^{List} ρ) **where**
from₀ Nil = M₁ (L₁ (M₁ U₁))
from₀ (Cons h t) = M₁ (R₁ (M₁ (K₁ h \times K₁ t)))
to₀ (M₁ (L₁ (M₁ U₁))) = Nil
to₀ (M₁ (R₁ (M₁ (K₁ h \times K₁ t)))) = Cons h t



Example: representing lists II

```
type Rep0List ρ =  
  D1 $List ( C1 $NilList U1  
             + C1 $ConsList (Par0 ρ × Rec0 (List ρ)))
```

And an instance of `Representable1` for kind $\star \rightarrow \star$ functions:

```
type Rep1List = D1 $List ( C1 $NilList U1  
                             + C1 $ConsList (Par1 × Rec1 List))
```

```
instance Representable1 List Rep1List where  
  from1 Nil           = M1 (L1 (M1 U1))  
  from1 (Cons h t) = M1 (R1 (M1 (Par1 h × Rec1 t)))  
  to1 (M1 (L1 (M1 U1)))           = Nil  
  to1 (M1 (R1 (M1 (Par1 h × Rec1 t)))) = Cons h t
```



Back to the library writer: generic map I

We show how to define `Functor` generically as an example of a kind $\star \rightarrow \star$ function. For consistency, we again use two type classes:

```
class Functor  $\phi$  where
```

```
  fmap :: ( $\rho \rightarrow \alpha$ )  $\rightarrow \phi \rho \rightarrow \phi \alpha$ 
```

```
class Functor1  $\phi$  where
```

```
  fmap1 :: ( $\rho \rightarrow \alpha$ )  $\rightarrow \phi \rho \rightarrow \phi \alpha$ 
```



Generic map II

The most interesting instance is the one for parameters:

instance Functor₁ Par₁ **where**
fmap₁ f (Par₁ a) = Par₁ (f a)

Recursion and composition rely on Functor:

instance (Functor ϕ) \Rightarrow Functor₁ (Rec₁ ϕ) **where**
fmap₁ f (Rec₁ a) = Rec₁ (fmap f a)

instance (Functor ϕ , Functor₁ ψ) \Rightarrow Functor₁ ($\phi \circ \psi$) **where**
fmap₁ f (Comp₁ x) = Comp₁ (fmap (fmap₁ f) x)



Generic map III

The default case applies the conversion functions:

$$\{-\# \text{DERIVABLE Functor fmap fmap}_{\text{Default}} \#-\}$$
$$\text{fmap}_{\text{Default}} :: (\text{Representable}_1 \phi \tau, \text{Functor}_1 \tau)$$
$$\Rightarrow \tau \rho \rightarrow (\rho \rightarrow \alpha) \rightarrow \phi \rho \rightarrow \phi \alpha$$
$$\text{fmap}_{\text{Default}} \text{rep } f \ x = \text{to}_1 (\text{fmap}_1 f (\text{from}_1 x \text{ 'asTypeOf' rep}))$$


Generic map III

The default case applies the conversion functions:

$$\{-\# \text{DERIVABLE Functor fmap fmap}_{\text{Default}} \#-\}$$
$$\text{fmap}_{\text{Default}} :: (\text{Representable}_1 \phi \tau, \text{Functor}_1 \tau)$$
$$\Rightarrow \tau \rho \rightarrow (\rho \rightarrow \alpha) \rightarrow \phi \rho \rightarrow \phi \alpha$$
$$\text{fmap}_{\text{Default}} \text{rep } f \ x = \text{to}_1 (\text{fmap}_1 f (\text{from}_1 x \text{ 'asTypeOf' rep}))$$

Now the compiler can derive **Functor** for **List**:

instance Functor List where

$$\text{fmap} = \text{fmap}_{\text{List}} (\perp :: \text{Rep}_1^{\text{List}} \rho) \text{ where}$$
$$\text{fmap}_{\text{List}} :: \text{Rep}_1^{\text{List}} \rho \rightarrow (\rho \rightarrow \alpha) \rightarrow \text{List } \rho \rightarrow \text{List } \alpha$$
$$\text{fmap}_{\text{List}} = \text{fmap}_{\text{Default}}$$


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- ▶ The deriving mechanism does not have to be “magic”: it can be explained in Haskell.
- ▶ Derivable functions become accessible and portable.
- ▶ We provide an implementation in UHC and detailed information on how to implement it for other compilers.
- ▶ We hope that the behavior of derived instances can be redefined in Haskell Prime, perhaps along the lines of our work.

