

Generic Generic Programming

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joint work with Andres Löh

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- ▶ Generic programming: an abstraction technique to reduce code duplication
 - ▶ Generic programs operate on “representation types”; a small set of types used to encode all other user-defined datatypes
 - ▶ Conversion functions mediate the isomorphism between a datatype and its generic representation

- ▶ Generic programming: an abstraction technique to reduce code duplication
 - ▶ Generic programs operate on “representation types”; a small set of types used to encode all other user-defined datatypes
 - ▶ Conversion functions mediate the isomorphism between a datatype and its generic representation
- ▶ Several generic programming libraries, specialised for different tasks, supporting different datatypes

class *GEq* ϕ where

geq :: ($\alpha \rightarrow \alpha \rightarrow \text{Bool}$) $\rightarrow \phi \alpha \rightarrow \phi \alpha \rightarrow \text{Bool}$

instance *GEq* *Unit* where *geq* _ *Unit* *Unit* = *True*

instance *Eq* $\alpha \Rightarrow$ *GEq* (*Arg* α) where *geq* _ (*Arg* x) (*Arg* y) = $x \equiv y$

instance *GEq* *Rec* where *geq* *eqf* (*Rec* x) (*Rec* y) = *eqf* $x y$

instance (*GEq* ϕ , *GEq* ψ) \Rightarrow *GEq* (ϕ :+ ψ) where

geq *eqf* (*Left* x) (*Left* y) = *geq* *eqf* $x y$

geq *eqf* (*Right* x) (*Right* y) = *geq* *eqf* $x y$

geq _ _ _ = *False*

instance (*GEq* ϕ , *GEq* ψ) \Rightarrow *GEq* (ϕ : \times ψ) where

geq *eqf* (x_1 : \times y_1) (x_2 : \times y_2) = *geq* *eqf* $x_1 x_2 \wedge$ *geq* *eqf* $y_1 y_2$

eq :: (*Regular* α , *GEq* (*Rep* α)) $\Rightarrow \alpha \rightarrow \alpha \rightarrow \text{Bool}$

eq $x y$ = *geq* *eq* (*from* x) (*from* y)

class *GEq* ρ ϕ where

geq :: $(\forall \iota. \rho \iota \rightarrow \tau \iota \rightarrow \tau \iota \rightarrow \text{Bool}) \rightarrow \rho \iota \rightarrow \phi \tau \iota \rightarrow \phi \tau \iota \rightarrow \text{Bool}$

instance *GEq* ρ *Unit* where *geq* $--$ *Unit* *Unit* = *True*

instance *Eq* $\alpha \Rightarrow$ *GEq* ρ (*Arg* α) where *geq* $--$ (*Arg* x) (*Arg* y) = $x \equiv y$

instance *El* $\rho \iota \Rightarrow$ *GEq* ρ (*Rec* ι) where

geq eqf $--$ (*Rec* x) (*Rec* y) = *eqf proof* x y

instance (*GEq* ρ ϕ , *GEq* ρ ψ) \Rightarrow *GEq* ρ (ϕ $:+:$ ψ) where

geq eqf p (*Left* x) (*Left* y) = *geq eqf* p x y

geq eqf p (*Right* x) (*Right* y) = *geq eqf* p x y

geq $--$ $--$ $--$ = *False*

instance (*GEq* ρ ϕ , *GEq* ρ ψ) \Rightarrow *GEq* ρ (ϕ $:x:$ ψ) where

geq eqf p (x_1 $:x:$ y_1) (x_2 $:x:$ y_2) = *geq eqf* p x_1 $x_2 \wedge$ *geq eqf* p y_1 y_2

instance *GEq* ρ $\phi \Rightarrow$ *GEq* ρ (ϕ $\triangleright:$ ι) where

geq eq p (*Tag* x) (*Tag* y) = *geq eq* p x y

eq :: (*Fam* ρ , *GEq* ρ (*Rep* ρ)) \Rightarrow $\rho \iota \rightarrow \iota \rightarrow \iota \rightarrow \text{Bool}$

eq p x y = *geq* $(\lambda p$ (*Io* x) (*Io* y) \rightarrow *eq* p x y) p (*from* p x) (*from* p y)

2010: generic-deriving



class *GEq* ϕ **where**

geq :: $\phi \alpha \rightarrow \phi \alpha \rightarrow \text{Bool}$

instance *GEq* *Unit* **where** *geq* *Unit* *Unit* = *True*

instance *Eq* $\alpha \Rightarrow$ *GEq* (*Arg* ι α) **where** *geq* (*Arg* x) (*Arg* y) = *geq* x y

instance (*GEq* α , *GEq* β) \Rightarrow *GEq* (α $:+$ β) **where**

geq (*Left* x) (*Left* y) = *geq* x y

geq (*Right* x) (*Right* y) = *geq* x y

geq $-$ $-$ = *False*

instance (*GEq* α , *GEq* β) \Rightarrow *GEq* (α $:×$ β) **where**

geq (x_1 $:×$ y_1) (x_2 $:×$ y_2) = *geq* x_1 x_2 \wedge *geq* y_1 y_2

eq :: (*Generic* α , *GEq* (*Rep* α)) \Rightarrow $\alpha \rightarrow \alpha \rightarrow \text{Bool}$

eq x y = *geq* (*from* x) (*from* y)

This is generic programming



- ▶ “Generic programming (...) makes it possible to write programs that solve a class of problems *once and for all*, instead of writing new code over and over again (...)” [Backhouse et al., 1999]
- ▶ “Generic programming techniques aim to *eliminate boilerplate* code.” [Lämmel and Peyton Jones, 2003]
- ▶ “Generic programming has developed as a technique for increasing the amount and scale of *reuse* in code (...)” [Jeuring et al., 2009]
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...yet generic programmers keep writing boilerplate code!

Duplicated representations across different libraries

Representing lists in regular:

```
instance Regular [α] where
  Rep [α] = Unit :+: ((Arg α) :×: Rec)
  from []      = Left Unit
  from (h : t) = Right (Arg h :×: Rec t)
  to (Left Unit)      = []
  to (Right (Arg h :×: Rec t)) = h : t
```

Representing lists in generic-deriving:

```
instance Generic [α] where
  Rep [α] = Unit :+: ((Arg P α) :×: (Arg (R S) [α]))
  from []      = Left Unit
  from (h : t) = Right (Arg h :×: Arg t)
  to (Left Unit)      = []
  to (Right (Arg h :×: Arg t)) = h : t
```

What should be possible

```
import Generics.Deriving           as GD  
import Generics.Regular.Rewriting as R  
import Generics.SYB.Schemes       as S  
import Conversions ()
```

```
data Logic  $\alpha$  = Var  $\alpha$  | Logic  $\alpha$  : $\forall$ : Logic  $\alpha$  | Not (Logic  $\alpha$ ) | T | F  
      deriving (GD.Generic)
```

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```

rewriting :: Logic Char

rewriting =

```

let elim2Not = R.rule $  $\lambda x \rightarrow$  Not (Not x) : $\rightsquigarrow$ : x
  
```

```

in R.bottomUp (R.rewrite elim2Not) $ T : $\forall$ : Not (Not (Var 'p'))
  
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```
size :: Int
```

```
size = S.everything (+) (const 1) $ Var 'p' : $\forall$ : Var 'q'
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```

    in R.bottomUp (R.rewrite elim2Not) $ T : $\forall$ : Not (Not (Var 'p'))
  
```

```

size :: Int
  
```

```

size = S.everything (+) (const 1) $ Var 'p' : $\forall$ : Var 'q'
  
```

```

rename :: Logic String
  
```

```

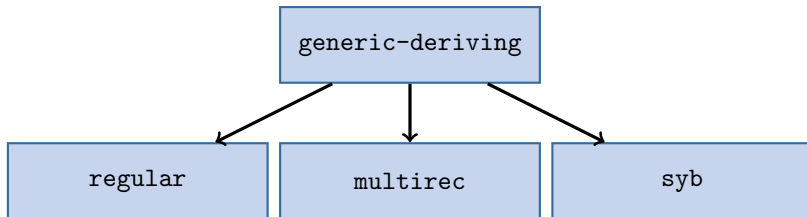
rename = GD.gmap ('_':) $ T : $\forall$ : Var "p"
  
```

Why?



- ▶ Reduce code duplication across generic programming libraries - generic generic programming!
- ▶ Reduce code size for generic representations
- ▶ Libraries can be specialised, and need not provide general functionality
- ▶ No need to rely on Template Haskell for automatically generating representations

How?



We use `generic-deriving` (which has built-in GHC support) to derive conversions to the other libraries.

A closer look at generic-deriving: Universe

```

kind UnivD = UnivD :+:D UnivD -- choice between constructors
             | UnivD :×:D UnivD -- multiple arguments
             | ArgD ArgType ★ -- arguments to constructors
             | UnitD -- datatypes without constructors

kind ArgType = P | R RecType | U -- parameter, recursion, or unknown
kind RecType = S | O -- self or other
  
```


A closer look at generic-deriving: Interpretation

```

data  $[[\alpha :: Univ_D]]_D :: \star$  where
  UnitD  ::                                $[[Unit_D]]_D$ 
  ArgD   ::  $\alpha$                            $\rightarrow [[Arg_D \iota \alpha]]_D$ 
  LeftD  ::  $[[\phi]]_D$                         $\rightarrow [[\phi :+:_D \psi]]_D$ 
  RightD ::  $[[\psi]]_D$                         $\rightarrow [[\phi :+:_D \psi]]_D$ 
  :×:D   ::  $[[\phi]]_D \rightarrow [[\psi]]_D$   $\rightarrow [[\phi :×:_D \psi]]_D$ 
  
```

A closer look at generic-deriving: Datatype instantiation

```
class GenericD ( $\alpha :: \star$ ) where  
  RepD  $\alpha :: \text{Univ}_D$   
  fromD  $:: \alpha \rightarrow \llbracket \text{Rep}_D \alpha \rrbracket_D$   
  toD    $:: \llbracket \text{Rep}_D \alpha \rrbracket_D \rightarrow \alpha$ 
```

A closer look at generic-deriving: Datatype instantiation

```

class GenericD ( $\alpha :: \star$ ) where
  RepD  $\alpha :: \text{Univ}_D$ 
  fromD  $:: \alpha \rightarrow \llbracket \text{Rep}_D \alpha \rrbracket_D$ 
  toD    $:: \llbracket \text{Rep}_D \alpha \rrbracket_D \rightarrow \alpha$ 
  
```

Example instance (lists):

```

instance Generic [ $\alpha$ ] where
  Rep [ $\alpha$ ] = UnitD  $:+:_D$  ((ArgD P  $\alpha$ )  $: \times :_D$  (ArgD (R S) [ $\alpha$ ]))
  from []      = LeftD UnitD
  from (h : t) = RightD (ArgD h  $: \times :_D$  (ArgD t))
  to (LeftD UnitD)           = []
  to (RightD (ArgD h  $: \times :_D$  (ArgD t))) = h : t
  
```

Comparison with regular



kind $Univ_R = Unit_R \mid Rec_R \mid Arg_R \star$
 $\mid Univ_R \text{ :+ : } R \quad Univ_R \mid Univ_R \text{ :x : } R \quad Univ_R$

Comparison with regular

kind $Univ_R = Unit_R \mid Rec_R \mid Arg_R \star$
 $\mid Univ_R \text{ :+ :}_R Univ_R \mid Univ_R \text{ :x :}_R Univ_R$

data $[\alpha :: Univ_R]_R (\tau :: \star)$ **where**

$Unit_R :: [\ Unit_R]_R \quad \tau$
 $Rec_R :: \tau \quad \rightarrow [\ Rec_R]_R \quad \tau$
 $Arg_R :: \alpha \quad \rightarrow [\ Arg_R \ \alpha]_R \quad \tau$
 $Left_R :: [\ \alpha]_R \ \tau \quad \rightarrow [\ \alpha \text{ :+ :}_R \ \beta]_R \ \tau$
 $Right_R :: [\ \beta]_R \ \tau \quad \rightarrow [\ \alpha \text{ :+ :}_R \ \beta]_R \ \tau$
 $(\text{:x :}_R) :: [\ \alpha]_R \ \tau \rightarrow [\ \beta]_R \ \tau \rightarrow [\ \alpha \text{ :x :}_R \ \beta]_R \ \tau$

Comparison with regular

kind $Univ_R = Unit_R \mid Rec_R \mid Arg_R \star$
 $\mid Univ_R \text{ :+}_R Univ_R \mid Univ_R \text{ :X}_R Univ_R$

data $[[\alpha :: Univ_R]]_R (\tau :: \star)$ where

$Unit_R :: [[Unit_R]]_R \tau$
 $Rec_R :: \tau \rightarrow [Rec_R]_R \tau$
 $Arg_R :: \alpha \rightarrow [Arg_R \alpha]_R \tau$
 $Left_R :: [[\alpha]]_R \tau \rightarrow [[\alpha \text{ :+}_R \beta]]_R \tau$
 $Right_R :: [[\beta]]_R \tau \rightarrow [[\alpha \text{ :+}_R \beta]]_R \tau$
 $(\text{:X}_R) :: [[\alpha]]_R \tau \rightarrow [[\beta]]_R \tau \rightarrow [[\alpha \text{ :X}_R \beta]]_R \tau$

class *Regular* $(\alpha :: \star)$ where

$Rep \alpha :: Univ_R$
 $from_R :: \alpha \rightarrow [[Rep \alpha]]_R \alpha$

From generic-deriving to regular: types

Our conversion from `generic-deriving` to `regular` consists of two steps:

- ▶ A type function *ToRegular* to convert the type representations
- ▶ A value-level function *toRegular* to convert the value accordingly

From generic-deriving to regular: types

Our conversion from generic-deriving to regular consists of two steps:

- ▶ A type function *ToRegular* to convert the type representations
- ▶ A value-level function *toRegular* to convert the value accordingly

ToRegular ($\alpha :: \text{Univ}_D$) :: Univ_R

ToRegular Unit_D = Unit_R

ToRegular ($\alpha :+:_D \beta$) = *ToRegular* $\alpha :+:_R$ *ToRegular* β

ToRegular ($\alpha :\times:_D \beta$) = *ToRegular* $\alpha :\times:_R$ *ToRegular* β

ToRegular ($\text{Arg}_D (R S) \tau$) = Rec_R

ToRegular ($\text{Arg}_D (R O) \alpha$) = $\text{Arg}_R \alpha$

ToRegular ($\text{Arg}_D P \alpha$) = $\text{Arg}_R \alpha$

ToRegular ($\text{Arg}_D U \alpha$) = $\text{Arg}_R \alpha$

From generic-deriving to regular: values

class *Convert_R* ($\alpha :: \text{Univ}_D$) τ **where**
toRegular :: $[[\alpha]]_D \rho \rightarrow [[\text{ToRegular } \alpha]]_R \tau$

instance *Convert_R* (*Arg_D* (*R S*) τ) τ **where**
toRegular (*Arg_D* x) = *Rec_R* x

instance *Convert_R* (*Arg_D* γ τ) ρ **where**
toRegular (*Arg_D* x) = *Arg_R* x

instance (*Convert_R* α τ , *Convert_R* β τ)
 \Rightarrow *Convert_R* (α $:+_D$ β) τ **where**
toRegular (*Left_D* x) = *Left_R* (*toRegular* x)
toRegular (*Right_D* x) = *Right_R* (*toRegular* x)

instance (*Convert_R* α τ , *Convert_R* β τ)
 \Rightarrow *Convert_R* (α $:x_D$ β) τ **where**
toRegular (x $:x_D$ y) = *toRegular* x $:x_R$ *toRegular* y

...

From generic-deriving to regular: datatypes

It is here that we set the second parameter of *Convert_R* to the type being converted (α):

```
instance (GenericD  $\alpha$ , ConvertR (RepD  $\alpha$ )  $\alpha$ )  $\Rightarrow$  Regular  $\alpha$  where  
  Rep  $\alpha$  = ToRegular (RepD  $\alpha$ )  
  fromR  $x$  = toRegular (fromD  $x$ )
```

With this instance, functions defined in the `regular` library are now available to all generic-deriving supported datatypes.

The Spine view (syb)

Encoding syb via the Spine view:

data *Spine* :: $\star \rightarrow \star$ **where**

Con :: $\alpha \rightarrow$ *Spine* α

$(:\diamond:)$:: (*Data* α) \Rightarrow *Spine* ($\alpha \rightarrow \beta$) $\rightarrow \alpha \rightarrow$ *Spine* β

class (*Typeable* α) \Rightarrow *Data* α **where**

spine :: $\alpha \rightarrow$ *Spine* α

instance (*Data* α) \Rightarrow *Data* [α] **where**

spine [] = *Con* []

spine ($h : t$) = *Con* (: $\diamond:$) $\diamond:$ h $\diamond:$ t

From generic-deriving to syb

Representing generic-deriving types as a Spine:

```
class ConvertS ( $\alpha :: \text{Univ}_D$ ) where
  toSpine ::  $[[\alpha]]_D \rightarrow \text{Spine } [[\alpha]]_D$ 
```

```
instance ConvertS UnitD where toSpine UnitD = Con UnitD
```

```
instance (ConvertS α, ConvertS β)  $\Rightarrow$  ConvertS (α :+:D β) where
  toSpine (LeftD x) = fmap LeftD (toSpine x)
  toSpine (RightD x) = fmap RightD (toSpine x)
```

```
instance (Data α)  $\Rightarrow$  ConvertS (ArgD ι α) where
  toSpine (ArgD x) = Con ArgD ∘ x
```

```
instance (GenericD α, ConvertS (RepD α), Typeable α)
   $\Rightarrow$  Data α where
  spine = fmap toD ∘ toSpine ∘ fromD
```

Further reading



In the paper we also have a conversion from `generic-deriving` to `multirec`.

Full code (compiling with GHC 7.6.2) available at
<http://dreixel.net/research/code/ggp.zip>.

Future work



- ▶ What is the performance penalty imposed by the conversions?
- ▶ Can we optimise it using “known techniques”?
- ▶ Which other libraries can we convert to?

We have:

- ▶ Recognised the existence of code duplication across generic programming libraries
- ▶ Eliminated this duplication by defining conversions between approaches
- ▶ Proposed a new approach to the development of generic programming, libraries, focusing on how to relate them to existing approaches, rather than reimplementing everything from scratch

Conclusion

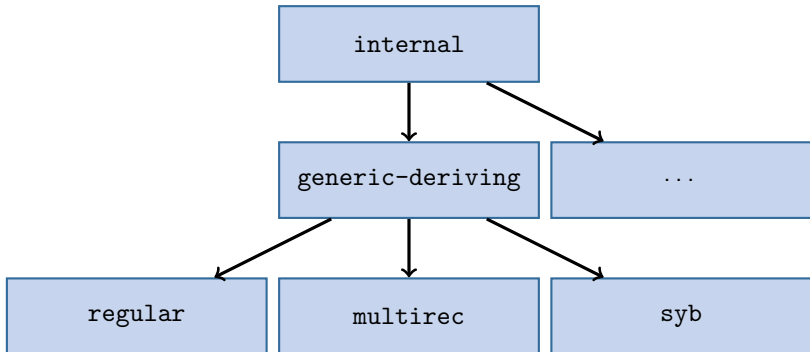


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Thank you for your time!

How?



Bibliography

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